Consider the differential equation

$$m\ddot{x} + c\dot{x} + kx = \sin(\omega t). \tag{1}$$

- \bigstar What is the **order** of this differential equation?
- ▲ Is this an autonomous differential equation or a non-autonomous differential equation?
- ▲ The term on the left represents a spring-mass-dashpot system as usual. What is the physical meaning of the term on the right side?
- ✓ Visit https://tinyurl.com/E911imitcycle2 and observe the dynamics at $\omega \approx 2$ and $\omega \approx 1/4$. Alternatively, you can visit https://emadmasroor.github.io/classes/E91_S25/Resources/ForcedHarmonicOscillator. nb to download the Mathematica notebook directly. Sketch x against time and \dot{x} against x for long times below. Let the initial condition for your plots be $x(0) = 1, \dot{x}(0) = 0$.



Consider the differential equation

$$+\mu (x^2 - 1) \dot{x} + x = 0.$$
⁽²⁾

▲ What is the **order** of this differential equation?

▲ Is this an autonomous differential equation or a non-autonomous differential equation?

 \ddot{x}

- ▲ Interpret the terms in this equation using the usual language of oscillators. What do they each mean?
- A For two values of $\mu = 0.1, 4$, and using the initial condition $x(0) = 1, \dot{x}(0) = 0$, numerically integrate these equations using a computer program of your choice, and sketch the resulting trajectories x(t). Use the accompanying graph paper to sketch what your computer program tells you. For $\mu = 0.1$, plot t = 0 to t = 100. For $\mu = 4$, plot t = 0 to t = 50.